A clinically practical algorithm has been developed for the treatment of liver cancer by the administration of rhenium-188 (\(^{188}\text{Re}\)-labeled lipiodol via the hepatic artery. This algorithm is based on the "maximum tolerated-activity" paradigm for radionuclide therapy. A small "scout" activity of \(^{188}\text{Re}\)-labeled lipiodol is administered to the patient before the actual therapeutic administration. At approximately 3 hours after administration, the activities in the normal liver, liver tumors, lungs, and total body are measured by gamma camera imaging using the conjugate-view method, with first-order corrections for attenuation (using a \(^{188}\text{Re}\) transmission scan) and scatter (using the "dual-window" method). At the same time, peripheral blood samples are counted, and the activity concentrations in whole blood are calculated. The blood activity concentrations are then converted to red marrow activity concentrations and then total red marrow activity using anatomic data from Standard Man anthropomorphic models. Next, the cumulated activities in the normal liver, liver tumors, lungs, red marrow, and total body are calculated using the measured activities in the respective source regions and conservatively assuming elimination of activity only by physical decay in situ. The absorbed doses to the therapy-limiting normal tissues, liver, lung, and red marrow, are then calculated using the Medical Internal Radiation Dose Committee schema, adjusting the pertinent S factors for differences in total body and organ masses between the patient and the anthropomorphic model and including the dose contribution from the liver tumors. Finally, based on maximum tolerated absorbed doses of 3,000, 1,200, and 150 rad (cGy) to liver, lung, and red marrow, the respective absorbed doses per unit administered activity are used to calculate the therapy activity. Although not required for treatment planning, tumor absorbed dose may also be estimated. This algorithm has been automated using an Excel (Microsoft, Redmond, WA) spreadsheet.

Historically, nuclear medicine has been largely a diagnostic specialty, and relatively low administered activities that are used diagnostically yield important clinical information whose benefit far outweighs the small potential risk associated with the attendant low normal-tissue absorbed doses. Average normal tissue doses for the "standard" patient, as found in package inserts for approved radiopharmaceuticals and in "reports" issued, for example, by the International Commission on Radiological Units, are therefore entirely adequate, although the tissue doses received by particular patients may deviate rather widely from such averages.

By incorporating appropriate radionuclides in appropriately large amounts into target tissue-avid radiopharmaceuticals, a sufficiently high radiation dose may be delivered to produce a therapeutic response in tumor or other target tissue, as in rhenium-188 (\(^{188}\text{Re}\)-labeled lipiodol therapy for the treatment of liver cancer. With such greater administered activities and resulting greater normal-tissue doses, serious radiation injury may ensue. It becomes critical, then, to determine at-risk normal tissue radiation doses with reasonable accuracy and precision. In conjunction with reliable dose-toxicity relationships for normal tissues, these dose estimates can be used to plan safe and effective radionuclide treatment for individual patients. Perhaps because of the greater accu-
racy and precision required, dosimetry methods for radionuclide therapy have not yet been standardized. This report describes a clinically practical algorithm for the treatment of liver cancer by hepatic artery administration of 188Re-labeled lipiodol based on the maximum tolerated activity. This algorithm has been automated using an Excel (Microsoft, Redmond, WA) spreadsheet, which performs the necessary calculations and incorporates the pertinent reference data.

Increasingly, to maximize the efficacy and minimize the toxicity of radionuclide therapy and in place of fixed-activity protocols, administered activities are customized to the individual patient. On the basis of kinetic measurements of “scout” activities and absorbed-dose calculations, individual patients will receive the maximum activity that will not exceed the radiation tolerance (ie, the tolerance absorbed dose) of normal tissue. Typically, perhaps only several normal tissues will be at significant risk, that is, likely to receive absorbed doses approaching their respective tolerance dose. For the treatment of metastatic thyroid cancer with iodide-131 (131I), for example, the therapeutic administered activity is that calculated to deliver no more than 200 rad to blood (as a surrogate for bone marrow).1-5 In radioimmunotherapy of non-Hodgkin’s B-cell lymphoma with 131I-labeled B1 anti-CD20 monoclonal antibody, on the other hand, the therapeutic administered activity is that delivering a dose of 75 rad to the total body (again as a surrogate for bone marrow).1-5

For 188Re-labeled lipiodol administered via the hepatic artery, the at-risk normal tissues are liver, lung, and red marrow and their respective tolerance absorbed doses are 3,000, 1,200, and 150 rad. Thus, for a particular patient, based on the empirically determined absorbed dose per unit administered activity (rad/mCi or cGy/MBq) to the liver, lung, and red marrow, the therapeutic administered activity will be the lowest value among those activities projected to deliver 3,000 rad to the liver, 1,200 rad to the lung, and 150 rad to the red marrow.

The dosimetry methodology described was used in a therapy trial conducted under the auspices of the International Atomic Energy Agency’s Thematic/Doctoral Coordinated Research Project, entitled “Management of Liver Cancer Using Radionuclide Methods With Special Emphasis on Trans-Arterial Radioconjugate Therapy and Internal Dosimetry.” The trial was unique in that a single protocol using a common labeling procedure for 188Re lipiodol and dosimetric methodology was conducted in 8 countries across 2 continents.

Physical Properties of 188Re

188Re, with a physical half-life ($T_{1/2}$) of 17 hours and physical decay constant ($\lambda_p$) of 0.041 hours, decays by negatron ($\beta$-ray) emission. The most abundant $\beta$-rays have maximum energies of 0.53 to 0.709 MeV and therefore ranges in water and soft tissue of $\sim$4 mm. Such relatively energetic $\beta$-rays are dosimetrically well-suited to treat primary liver tumors. Their relatively long range, $\sim$4 mm, means that tumors will be rather uniformly irradiated. At the same time, because such tumors typically have dimensions of at least several centimeters at the time of treatment, these $\beta$-rays will be completely absorbed within the tumors. As usual, therefore, the tumor-to-tumor, or “self-irradiation,” $\beta$-ray absorbed fraction will be one, $\phi_{\beta}(\text{tumor} \rightarrow \text{tumor}) = 1$, where “np” indicates “nonpenetrating” radiation (ie, particulate radiations such as $\beta$-rays).

In addition, 188Re emits a 155-keV $\gamma$-ray in 15% of its decays as well as 478- and 633-keV $\gamma$-rays (2.3%). For dosimetry measurements, the 155-keV $\gamma$-ray, comparable in energy with the 140-keV $\gamma$-ray of technetium-99m ($^{99m}$Tc), can be imaged with a conventional gamma camera using a standard 20% photopeak energy window, 155 keV $\pm$ 10% = 150 to 171 keV. A low-energy collimator, however, would not be suitable for imaging 188Re. Although low in abundance, the scattered 478- and 633-keV $\gamma$-rays would penetrate such a collimator and thus degrade the image by contributing a relatively large number of “uncollimated,” mispositioned counts to the 188Re image. Although high-energy collimation would minimize this effect, the associated reduction in sensitivity might be prohibitive since the 155-keV $\gamma$-rays are emitted in only 15% of 188Re decays. Thus, medium-energy collimation is probably the optimum choice for imaging 188Re. Depending on the make and model of the gamma camera, the so-called “front-end” (ie, preamplifier, amplifier, and/or high-voltage) settings used for $^{99m}$Tc can probably be used for 188Re. On the other hand, a separate sensitivity or uniformity (flood) correction map (table) probably should be acquired and used for 188Re. Further, in contrast to conventional practice, a system 188Re correction map, that is, a correction map using a flood, rather than a point, source of 188Re and with collimation in place, should be acquired. In this way, the confounding effects of the 478- and 633-keV $\gamma$-rays can be accounted for.

Pharmacokinetics and Cumulated Activities of $^{188}$Re-Labeled Lipiodol

After the administration of 188Re-labeled lipiodol into the hepatic artery, uptake in liver tumors and in at-risk normal tissues, such as liver and lung, is rapid. The subsequent clearance of lipiodol is remarkably slow (biological clearance half-times range from $\sim$8 days in tumor to $\sim$13 days in lung and liver) and, other than liver, tumor, and lung, there are no notable sites of lipiodol accumulation. The appearance of activity in blood and therefore presumably in red marrow is somewhat slower but still rapid, generally reaching maximal or near-maximal levels by 3 to 4 hours after administration. Therefore, relative to the 17-hour physical half-life of 188Re, uptake may be considered instantaneous followed by elimination only by physical decay in situ (ie, there is negligibly slow biological elimination) in blood (red marrow) as well as in liver and lung. This means that 188Re activity in the respective tissues (source regions) follows monoeponential kinetics in which (1) the zero-time-activity can be reliably estimated for liver and lung from scintigraphic images acquired anytime up to $\sim$3 hours after administration and for red marrow obtained at $\sim$3 hours and (2) the effective clearance...
constant (or half-times) equals the physical decay constant (or half-time):  
\[ \Lambda_0(t) = (\Lambda_0)h e^{-(\lambda_p)h t} \]  

(1)

where \( \Lambda_0(t) \) = the activity in source region \( r_h \) at time \( t \) after administration;  
\( (\Lambda_0)h \) = the zero-time activity (uptake) in source region \( r_h \), 
\( \approx \Lambda_0(3 \text{ hours}) \);  
\( (\lambda_p)h \) = the effective clearance constant of activity in source region \( r_h \)  
\[ = \lambda_p + (\lambda_b)h \]  

(2a)

\[ \approx \lambda_p \]  

(2b)

\[ = 0.041/\text{hr} \text{ for } ^{188}\text{Re} \]  

(2c)

where \( \lambda_p \) = the physical decay constant of the radionuclide  
\[ = 0.041/\text{hr} \text{ for } ^{188}\text{Re} \]  

(3)

and \( (\lambda_b)h \) = the biological clearance constant from source region \( r_h \).

The resulting monoexponential kinetics, in turn, greatly simplify the estimation of cumulated activities. (The subscripts “1/2,” has been eliminated to make the equations less unwieldy.)

\[ \bar{\Lambda}_h = \frac{(\Lambda_0)h}{(\lambda_p)h} \]  

(4a)

\[ \approx \frac{(\Lambda_0)h}{\lambda_p} \]  

(4b)

\[ = 1.44 \text{ (}\Lambda_0)h \text{ (Te)}_h \]  

(4c)

\[ = 1.44 \text{ (}\Lambda_0)h \text{ (}T_p\text{)}_h \]  

(4d)

where \( \text{Te} = \text{the effective half-life} \)  
\( T_p = \text{the physical half-life} \)  
\[ = 17 \text{ hours for } ^{188}\text{Re} \]  

(5)

Although consistent with the measured kinetics of \(^{188}\text{Re}-\)labeled lipiodol, the assumptions of instantaneously uptake and elimination only by physical decay in situ are nonetheless conservative. That is, these assumptions tend to yield estimates of cumulated activities and therefore absorbed doses per unit administered activity that are likely somewhat greater than the actual values. In turn, the calculated therapeutic administered activity will be slightly lower than the actual maximum-tolerated activity. However, given the large uncertainties in estimating absorbed doses from internal radionuclides, it is probably desirable to err on the side of safety.

**Source- and Target-Region Masses**

For \(^{188}\text{Re}-\text{lipiodol}, the source regions are liver, lung, red marrow, and the rest of the body, and the pertinent target regions are liver, lung, and red marrow. In addition to total body mass, liver and tumor masses (in g) are required for each patient before treatment. The most expeditious and accurate approach to liver and volumetrics is either the use of computed tomography (CT) or magnetic resonance imaging (MRI). The CT or MRI images themselves are not required for dosimetry—only the estimates of the liver and masses. For purposes of treatment planning, gamma camera imaging in general and planar gamma camera imaging in particular are not really adequate for such volumetric measurements. Measurement of patient-specific lung and red marrow masses are not required because the effect of mass on the respective S factors can be reasonably approximated using the patient’s total-body mass (see below “Calculation of Absorbed Doses: The Medical Internal Radiation Dose Committee (MIRD) Scheme”). On the other hand, measurement of the liver and the intrahepatic lesions is required not only because these lesions are critical source and target regions but also because they may significantly distort the overall size and shape of the liver. On each transverse CT or MR image j on which the liver and/or the liver tumors appear, regions of interest (ROIs) may be manually drawn around the entire liver (including the tumors) and around each individual lesion. The masses of the entire liver (including the tumors) and each tumor are then calculated:

\[ \text{Mass of region i (g)} \]

\[ = \sum_{\text{Image j}} \text{Area of region i in image j (pixels)} \times \text{Pixel area (mm}^2\text{)} \times \text{Image thickness (mm)} \times \rho(\text{g/cm}^3) \times 0.001 \text{ cm}^3/\text{mm}^3 \]  

(6)

The mass of the normal liver (ie, the entire liver excluding the liver tumors) can then be calculated:

\[ \text{Mass of normal liver (g)} \]

\[ = \text{Mass of entire liver (g)} - \sum_{\text{Liver tumors k}} \text{Mass of liver tumor k (g)} \]  

(7)

An analogous ROI analysis can be applied to the gamma camera images to determine the activities and cumulated activities specifically in the normal liver and the tumor(s).

**Source-Region Time-Activity Data**

As discussed previously, because of the rapid uptake and subsequent slow clearance of lipiodol relative to the 17-hour physical half-life of \(^{188}\text{Re}, measurement of liver, lung, and total-body activities can be performed anytime from 1 to 3 hours after administration to yield the respective “zero-time” source-region activities. Blood sampling, on the other hand, should not be performed before \( \sim 3 \) hours after administration. All activity or activity concentration measurements must be corrected for radioactive
Quantitation of activity in red marrow presents a special problem in radionuclide dosimetry in that it is widely distributed source region that cannot be assayed in its entirety. At that same time, there may be wide variability in activity concentrations in marrow, and biopsy and counting of activity in a marrow sample are therefore prone to sampling error. A simple practical approach is to calculate the red marrow activity concentration as follows:

\[
\text{Activity concentration (\(\mu\text{Ci/g}\)) in red marrow} = \frac{\text{Red marrow extracellular fluid fraction} \times \text{Activity concentration (\(\mu\text{Ci/g}\)) in blood}}{1 - \text{Hematocrit}} (8)
\]

For purposes of radionuclide dosimetry, the American Association of Physicists in Medicine has recommended a value of 0.4 for the red marrow extracellular fluid fraction whereas Sgouros has recommended a value of 0.2. The more conservative value of 0.4, which yields a greater red marrow activity concentration, should be used.

Finally, the total activity in red marrow is calculated using the total mass of red marrow in the 70-kg reference man (1,500 g) or 54-kg reference woman (1,300 g) anthropomorphic models for male or female patients, respectively:

\[
\text{Activity (\(\mu\text{Ci}\)) in red marrow} = \text{Total mass (g) of red marrow} \times \text{Activity concentration (\(\mu\text{Ci/g}\)) in red marrow} (9)
\]

\(^{188}\text{Re} \) activities in the liver, lung, and the rest of the body can be measured by planar gamma camera imaging using the conjugate-view method with first-order corrections for scatter and attenuation. Optimal, this is performed using a dual-detector gamma camera with whole-body scanning capability.

**Scatter Correction**

“Small-angle” Compton scatter, which is abundant in a distributed radioactive source such as a patient, diverts emitted x- and \(\gamma\)-rays from their original direction of travel without reducing their energy to the point that it lies below the photopeak energy window. As a result, mispositioned events are included in the gamma camera image. Although important for activity quantitation, rigorous scatter correction is complex. However, Jaszczak and coworkers have developed a straightforward scatter correction method, the so-called “dual-window” method, that can be easily implemented on most modern gamma camera systems. As illustrated in Figure 1, the dual-window scatter correction requires simultaneous acquisition of 2 separate images, corresponding to photopeak (conventional) and scatter energy windows, respectively.

The scatter-corrected image is then derived as follows:

\[
\text{Scatter-corrected image} = \text{Photopeak energy window image} - 0.5 \times \text{Scatter energy window image} (10)
\]

In all subsequently described image analyses, the scatter corrected images are used.

**Attenuation Correction**

Attenuation of the 115-keV \(\gamma\)-rays emitted by \(^{188}\text{Re} \) in vivo will be substantial and highly variable, depending on the size (ie, thickness) of the patient and of different internal organs of the patient and the composition (soft tissue, bone, lung [ie, air]) of the overlying tissue. Mean attenuation correction factors should therefore be measured for the pertinent source regions, the liver and liver tumors, lung, and the total body, as illustrated in Figure 2. A flood source is filled with a uniform ~10-mCi solution of \(^{188}\text{Re} \) and placed on the lower gamma camera detector. With the scanning table in place but without the patient, a “whole-body” scan of the flood source is acquired with the same scan speed, scan length, and detector separation as will be used for the transmission scan. Before the administration of radioactivity to the patient, a \(^{188}\text{Re} \) transmission scan...
through the patient is acquired; the administration of the $^{188}$Re-labeled lipiodol and subsequent $^{188}$Re imaging should be performed without moving the patient. Mean attenuation correction factors for the pertinent source regions, the liver and liver tumors, lung, and total body, are then formed from the 2 upper detector scans by region-of-interest (ROI) analysis:

$$\text{Mean attenuation correction factor for source region } r_h \approx \sqrt{\frac{\text{Mean counts per pixel in source region } r_h \text{ ROI on the upper detector flood source scan}^*}{\text{Mean counts per pixel in source region } r_h \text{ ROI on the upper detector transmission scan}^*}}$$

(11)

*Scatter-corrected image.

The ROI for the liver and liver tumors can be manually drawn on the subsequently acquired $^{188}$Re images of the patient and the lung and total body ROIs on the transmission scan.

**Scatter-corrected, mirrored image.

Conjugate-View Imaging

Once the patient has been injected with the $^{188}$Re-labeled lipiodol, a calibrated standard source of $^{188}$Re is placed on the patient’s scanning table adjacent to but not on the patient and a whole-body scan performed (Fig. 3).

Both the upper- and lower-detector images should be corrected for scatter (see Fig. 3 and Eq. 10), the scatter-corrected lower-detector image “mirrored” to align it with the upper detector image, and the geometric mean image formed:

$$\text{Geometric-mean image} = \sqrt{\text{Upper-detector image}^* \times \text{Lower-detector image}^{**}}$$

(12)

Calculating the absorbed dose:

$$\text{Activity (}\mu\text{Ci}) \text{ in source region } r_h \approx \frac{\text{Total pixels in source region } r_h \text{ ROI} \times \left(\frac{\text{Mean counts per pixels in source region } r_h \text{ ROI} - \text{Mean counts per pixel in background ROI}}{\text{Activity (}\mu\text{Ci}) \text{ in calibrated standard ROI}}\right)}{\text{Mean counts per pixel in background ROI}}$$

(13)

Finally, the activity ($\mu\text{Ci}$) in each of the pertinent source regions $r_h$, liver, tumor(s), lung, and total body, is calculated using ROI analysis of the geometric-mean image:

$$\text{Conjugate-View Imaging}$

Figure 2 Setup for gamma camera imaging for measurement of mean attenuation correction factors. As in conventional whole-body scanning, the upper and lower detectors are translated together relative to the patient scanning table. (Color version of figure is available online.)

Figure 3 Set-up for conjugate-view whole-body scanning following administration of the $^{188}$Re-labeled lipiodol, with a $^{188}$Re-calibrated standard ($\sim 100 \mu\text{Ci}$) in the field of view. (Color version of figure is available online.)
activity (ie, cumulated activity) in source region rh, is as follows:  

\[ \bar{D}(r_h \leftarrow r_h) = \frac{\tilde{A}_h \sum_i \Delta_i \phi_i(r_h \leftarrow r_h)}{M_k} \]  

(15a)

\[ = \tilde{A}_h \sum_i \Delta_i \phi_i(r_h \leftarrow r_h) \]  

(15b)

\[ = \tilde{A}_h S(r_h \leftarrow r_h) \]  

(15c)

\( \tilde{A}_h \) = the cumulated activity in source region rh, that is, the total number of decays in source region rh,

\( M_k \) = the mass of target region rk,

\( \Delta_i \) = the equilibrium dose constant for radiation i, that is, the average energy emitted per decay in the form of radiation i (see reference 10 for a comprehensive tabulation),

\( \phi_i(r_h \leftarrow r_h) \) = the absorbed fraction in target region rk for radiation i emitted in source region rh, that is, the fraction of energy of radiation i emitted in source region rh that is absorbed in target region rk,

\( \Phi_i(r_h \leftarrow r_h) \) = the specific absorbed fraction in target region rk for radiation i emitted in source region rh, that is, the fraction of energy of radiation i emitted in source region rh that is absorbed per unit mass in target region rk,

\[ = \frac{\phi_i(r_h \leftarrow r_h)}{M_k}, \]  

(16)

and \( S(r_h \leftarrow r_h) \) = the radionuclide-specific S factor for target region rk and source region rh, that is, the absorbed dose to target region rk per unit cumulated activity in source region rh,

\[ \sum_i \Delta_i \phi_i(r_h \leftarrow r_h) \]  

(17)

The total mean absorbed dose \( \bar{D}(r_h) \) to target region rh is then calculated by summation of the absorbed dose contributions from all source regions rh:

\[ \bar{D}(r_h) = \tilde{A}_h \sum_i \Delta_i \phi_i(r_h \leftarrow r_h) \]  

(18a)

\[ = \sum_h \left[ \tilde{A}_h \sum_i \Delta_i \phi_i(r_h \leftarrow r_h) \right] \]  

(18b)

\[ = \sum_h \left[ \tilde{A}_h S(r_h \leftarrow r_h) \right] \]  

(18c)

See Tables 1 and 2 for a tabulation of the standard anthropomorphic models used in the MIRD schema and selected \(^{188}\)Re S factors for the 70-kg standard man model, respectively.

The cumulated activity, \( \tilde{A}_h \), in each pertinent source region rh, liver, lung, red marrow, and total body, is calculated from Eq. (4b) using the respective zero-time activities, \( (\text{A}_0)_h \), given by Eq. (9) for red marrow and by Eq. (14) for liver, lung, and total body. Finally, the rest-of-body cumulated activity can be calculated by subtracting the liver, lung, and red marrow cumulated activities from the total body cumulated activity.

### Adaptation of the MIRD Schema to Patient-Specific Dosimetry

Although the standard anthropomorphic models used in the MIRD schema represent normal human anatomy and thus do not include tumors, the schema can be adapted to patient-specific normal-organ dosimetry for planning radionuclide therapy based on the maximum-tolerated activity.  

This is the approach adopted for \(^{188}\)Re-labeled lipiodol treatment of liver cancer. Not surprisingly, the most important quantitative adjustment in this adaptation involves the tumor-bearing organ(s), in this case, the liver.

For organ “non-self” irradiation (source region rh \( \neq \) target region rk), S factors are relatively insensitive to organ (ie, source- and target-region) size and shape. Therefore, unless the source and/or target regions are grossly abnormal (eg, because of the presence of tumors), the reference man (or reference woman) S factors may be applied to specific patients for calculating the organ non-self absorbed dose contribution:

\[ S(r_h \leftarrow r_h) \approx S(r_h \leftarrow r_h) \]  

(19)

\[ \text{if } r_h \neq r_k \]

For organ “self” irradiation (source region rh = target region rk), S factors are approximately inversely proportional to organ mass because most of the self-dose to any organ is contributed by nonpenetrating radiations that are completely absorbed locally regardless of the organ mass whereas absorbed dose, by definition, is inversely proportional to the organ mass. Therefore, for normal organ (ie, organs without tumor), S factors adjusted for the difference in mass between the patient and reference-man organ may be applied to specific patients for calculating the self absorbed dose contribution:

\[ S(r_h \leftarrow r_h) \approx S(r_h \leftarrow r_h) \times \frac{\text{Reference-man target-region } (r_k) \text{ mass}}{\text{Patient target-region } (r_h) \text{ mass}} \]  

(20a)

\[ \text{if } r_h = r_k \]

In principle, patient organ masses may be estimated with CT or MRI. In practice, however, masses of normal organs may not be available. A more practical, though less accurate, adaptation of Eq. (18a) based on the patient and reference man total-body masses may then be used:
For a tumor-bearing organ, in the case of $^{188}$Re-labeled lipiodol therapy, the liver, adaptation of the MIRD schema is somewhat more complicated. First, the self-irradiation absorbed dose and S factor for the tumor-bearing organ can be separated into their penetrating and nonpenetrating radiation components:

$$D(r_h \leftarrow r_k) = D_p(r_h \leftarrow r_k) + D_{np}(r_h \leftarrow r_k) \quad (21)$$

$$S(r_h \leftarrow r_k) = S_p(r_h \leftarrow r_k) + S_{np}(r_h \leftarrow r_k) \quad (22a)$$

Table 2

<table>
<thead>
<tr>
<th>Target Region, $r_k$</th>
<th>Liver</th>
<th>Lung</th>
<th>Red Marrow</th>
<th>Other Tissue (Muscle)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Liver</td>
<td>$9.5 \times 10^{-4}$</td>
<td>$9.1 \times 10^{-7}$</td>
<td>$3.6 \times 10^{-7}$</td>
<td>$4.1 \times 10^{-7}$</td>
</tr>
<tr>
<td>Lung</td>
<td>$9.4 \times 10^{-7}$</td>
<td>$1.7 \times 10^{-3}$</td>
<td>$4.5 \times 10^{-7}$</td>
<td>$5.0 \times 10^{-7}$</td>
</tr>
<tr>
<td>Red marrow</td>
<td>$5.0 \times 10^{-7}$</td>
<td>$6.0 \times 10^{-7}$</td>
<td>$7.5 \times 10^{-4}$</td>
<td>$6.4 \times 10^{-7}$</td>
</tr>
</tbody>
</table>

Adapted from Snyder et al. 21
radiation $i$, nonpenetrating radiations for source and target region $r_h$, and $<H9004$/H9004$>, where
\[ S(r_h \leftarrow r_h) = S(r_h \leftarrow r_h) + \sum_i (\Delta_{np})_i \cdot (d_{np})_i \cdot (r_h \leftarrow r_h) \quad (22b) \]
\[ S_p(r_h \leftarrow r_h) = \sum_i (\Delta_{np})_i \quad (22c) \]
\[ S_p(r_h \leftarrow r_h) = \frac{\Delta_{np}}{M_h} \quad (22d) \]

where
\[ S(r_h \leftarrow r_h) = \text{the total self-irradiation S factor in source and target region } r_h, \]
\[ = 9.4 \times 10^{-4} \text{rad/µCi-hr for } ^{188}\text{Re} \text{ in the reference-man normal liver} \quad (23) \]

\[ S_p(r_h \leftarrow r_h) = \text{the self-irradiation S factor for penetrating radiations in source and target region } r_h, \]
\[ S_{np}(r_h \leftarrow r_h) = \text{the self-irradiation S factor for nonpenetrating radiations in source and target region } r_h, \]
\[ (\Delta_{np})_i = \text{the equilibrium dose constant for nonpenetrating radiation } i, \]
\[ (d_{np})(r_h \leftarrow r_h) = \text{the self-irradiation absorbed fraction in nonpenetrating radiations for source and target region } r_h, \]
\[ = 1, \]
\[ M_h = \text{the mass of the source and target region } r_h, \]
\[ = 1,800 \text{ g for the reference-man normal liver,} \quad (24) \]

and $\Delta_{np}$ = the total equilibrium dose constant for nonpenetrating radiations
\[ = \sum_i (\Delta_{np})_i \]
\[ = 1.66 \text{ g-rad/µCi-hr for } ^{188}\text{Re.} \quad (25) \]

Therefore,
\[ S_p(r_h \leftarrow r_h) = S(r_h \leftarrow r_h) - \frac{\Delta_{np}}{M_h} \quad \text{and} \quad (26a) \]
\[ S_p(\text{Normal liver} \leftarrow \text{Normal liver}) = 1.78 \times 10^{-5} \text{ rad/µCi-hr} \quad (26b) \]

for $^{188}\text{Re}$ in the reference-man normal liver.

Using Eq. (18a) for $^{188}\text{Re}$ in the liver, that is, in the normal liver and, the patient-specific self-irradiation S factor for penetrating radiations can then be calculated as follows:

\[ \text{Patient} \]
\[ S_p(Liver \leftarrow Liver) = 1.78 \times 10^{-5} \text{ rad/µCi-hr} \]
\[ \times \frac{1800 \text{ g}}{\text{Patient liver mass}} \quad (27b) \]
\[ = \frac{0.032}{\text{Patient liver mass}}. \quad (27c) \]

For $^{188}\text{Re}$ in the liver, this is, in the normal liver and tumor, the patient-specific self-irradiation absorbed dose for penetrating radiations is therefore:
\[ D_p(\text{Normal Liver} \leftarrow \text{Normal Liver}) \]
\[ \approx S_p(\text{Liver} \leftarrow \text{Liver}) \times \tilde{A}_{\text{Liver}} \quad (28a) \]
\[ \text{Patient} \]
\[ = S_p(\text{Liver} \leftarrow \text{Liver}) \times \tilde{A}_{\text{Liver}} \quad (28b) \]
\[ \text{Patient} \]
\[ = S_p(\text{Liver} \leftarrow \text{Liver}) \times \{\tilde{A}_{\text{Normal Liver}} + \tilde{A}_{\text{Tumor}}\}. \quad (28c) \]

The self-irradiation absorbed dose for nonpenetrating radiations in source and target region $r_h$ is:
\[ D_{np}(r_h \leftarrow r_h) = \frac{\Delta_{np}}{M_h} \times \tilde{A}_{h} \quad (29) \]

For $^{188}\text{Re}$ in the liver, therefore, the mean patient-specific self-irradiation absorbed dose to the normal liver for nonpenetrating radiations is:
\[ D_{np}(\text{Normal liver} \leftarrow \text{Normal liver}) \]
\[ = \frac{\Delta_{np}}{\text{Patient normal liver mass}} \times \tilde{A}_{\text{Normal liver}}. \quad (30) \]

The total absorbed dose to the patient normal liver is simply the sum of $D_p(\text{Normal liver} \leftarrow \text{Normal liver})$, given in Eqs. (27c) and (28c), and $D_{np}(\text{Normal liver} \leftarrow \text{Normal liver})$, given in Eq. (30).

Note that the absorbed dose to the normal liver from penetrating radiations (x- and γ-rays) includes contributions from activity in both the normal liver and from tumor in the liver because of the relatively long distances penetrated by such radiations. In contrast, the absorbed dose from nonpenetrating radiations (β-rays) is contributed only by activity in the normal liver itself because such radiations are completely absorbed within the tumor, that is, cannot penetrate into the surrounding normal liver.

The absorbed dose contribution from activity in the rest of the body, that is, not specifically in the liver, lung, and red marrow, also should be included. Muscle, of course, is a tissue distributed throughout the body, and the respective S factors with muscle as the source region can be used to estimate the absorbed dose contributions from the rest of the body to liver, lung, and red marrow:
\[ S(r_h \leftarrow \text{Rest of body}) \approx S(r_h \leftarrow \text{Muscle}) \quad (31) \]
The cumulated activity in the rest of the body can be calculated by subtracting the combined cumulated activities in the liver, lung, and red marrow from that in the total body. The total absorbed doses, D(Normal liver), D(Lung), and D(Red marrow), to the respective at-risk normal tissues, liver, lung, and red marrow, are then calculated by summing the source region absorbed dose contributions:

\[
\begin{align*}
D(\text{Normal liver}) &= D(\text{Normal liver} \leftarrow \text{Normal liver with tumor}) \\
&+ D(\text{Liver} \leftarrow \text{Lung}) \\
&+ D(\text{Liver} \leftarrow \text{Red marrow}) \\
&+ D(\text{Liver} \leftarrow \text{Rest of body}) \\
D(\text{Lung}) &= D(\text{Lung} \leftarrow \text{Normal liver with tumors}) \\
&+ D(\text{Lung} \leftarrow \text{Lung}) \\
&+ D(\text{Lung} \leftarrow \text{Red marrow}) \\
&+ D(\text{Lung} \leftarrow \text{Rest of body}) \\
D(\text{Red marrow}) &= D(\text{Red marrow} \leftarrow \text{Normal liver with tumors}) \\
&+ D(\text{Red marrow} \leftarrow \text{Lung}) \\
&+ D(\text{Red marrow} \leftarrow \text{Red marrow}) \\
&+ D(\text{Red marrow} \leftarrow \text{Rest of body})
\end{align*}
\]

(32a)

The total absorbed doses to the at-risk normal tissues are then normalized to the scout administered activity (mCi) to yield the respective absorbed doses per unit administered activity (rad/mCi). Based on the absorbed doses per unit administered activity (rad/mCi) thus calculated, the actual therapeutic activity to be administered is the minimum value among those activities projected to deliver the maximum tolerated absorbed doses to the respective at-risk normal tissues—3,000 rad to liver, 1,200 rad to lung, and 150 rad to red marrow.

\[
\begin{align*}
D(\text{Tumor} \leftarrow \text{Tumor}) &= D_p(\text{Tumor} \leftarrow \text{Tumor}) \\
&+ D_{np}(\text{Tumor} \leftarrow \text{Tumor}) \\
&= 0.0346 \times \Gamma \times \bar{G} \times T_p \times (A_{\text{tumor}}) \frac{\Delta_{np}}{\text{Tumor mass}} + \frac{\Delta_{np}}{\text{Tumor mass}} \times \bar{T}_{\text{Tumor}}
\end{align*}
\]

(33b)

where \(D(\text{Tumor} \leftarrow \text{Tumor})\) = the self-dose, that is, the tumor-to-tumor absorbed dose,
\(D_p(\text{Tumor} \leftarrow \text{Tumor})\) = the self-dose, that is, the tumor-to-tumor absorbed dose, for penetrating raduations,
\(D_{np}(\text{Tumor} \leftarrow \text{Tumor})\) = the self-dose, that is, the tumor-to-tumor absorbed dose, for nonpenetrating raduations,
\(\Gamma\) = the specific gamma ray constant (rad-cm²/μCi-h),
\(\bar{G}\) = the mean geometric factor

\[
= 3\pi r^2
\]

(34)

where \(r\) = the radius (cm) of the tumor (assumed to be spherical).

As noted previously, the entire algorithm has been automated using an Excel spreadsheet, which performs the necessary calculations and incorporates all the pertinent reference data.

**Conclusion**

Radiation dosimetry deals with the determination of the amount and the spatial and temporal distribution of energy deposited in matter by ionizing radiation. Internal radionuclide radiation dosimetry specifically deals with the deposition of radiation energy in tissue due to a radionuclide within the body. However, unlike external radiation dose (which can often be measured), internal radiation dose must be calculated. These procedures have evolved for more than 60 years from relatively simple approaches to those with a high level of sophistication. This report has presented the basic concepts and practical computational approaches to patient-specific internal radiation dosimetry for intrahepatic artery 188Re-labeled lipiodol for treatment of liver cancer. Although conceptually straightforward, the computations presented are tedious. Importantly, beginning with CT- or MRI-derived organ and masses, and organ and total-body activities (from gamma camera imaging) as input data, all pertinent calculations can be performed with an Excel spreadsheet. Further, all necessary reference data (eg, reference-man organ masses, equilibrium dose constants, S factors) are readily available and can be incorporated into such a spreadsheet to fully automate the dose-calculation process.

Intrahepatic artery lipiodol localizes in liver tumors and, when labeled with 131I, is efficacious in their treatment. It is expensive and not widely available, especially in the developing parts of the world in which liver cancer is endemic. Lipiodol labeled with generator-produced, \(\beta\)-emitting 188Re (17 hours; \(E_{\beta} = 0.53-0.70\) MeV; range = 4 mm), is a convenient, cost-effective alternative. The 188Re-lipiodol dosimetry protocol described has been implemented worldwide in the International Atomic Energy Agency’s Coordinated Research Project on radionuclide treatment of liver cancer. As described in detail elsewhere in this issue, the trial in which this dosimetry methodology was employed comprised 185 patients from 8 countries, including China, Colombia, India, Mongolia, the Philippines, Singapore, Thailand, and Vietnam. Patient age ranged from 22 to 84 years (median 55 years, mean 55.4 years, SD 11.8 years). There were 146
(79%) men and 39 (21%) women. Of the 185 patients, to date 145 have sufficient information available for dosimetric analysis. A single treatment was given to 134 patients (72%), 42 patients (23%) received 2 treatments, 8 (4%) received 3 treatments, and 1 patient received 4 treatments. The total administered activity (including the scout dose) during the first treatment ranged from 21 to 363 mCi (mean: 108 mCi, median 100 mCi; SD 54 mCi). In 32% of the patients, the dose-limiting organ was the lungs whereas in the other 68%, it was the liver. In all the patients that received less than the maximum dose to lungs or liver, there was no dose-limiting toxicity. Only one patient received more than the maximum pulmonary radiation absorbed dose; there was transient pulmonary toxicity in this patient. Two other patients developed pulmonary toxicity after the second treatment dose; the cumulative pulmonary radiation absorbed dose in these patients was less than the maximum permissible dose. However, the effect of cumulative radiation to the lungs cannot be estimated from the available data. Moreover, several factors, including baseline performance status and extent of disease and pulmonary function before each treatment, as well as interval between treatments, will effect pulmonary toxicity. With basic instrumentation (planar gamma camera, well counter) available in most developing countries, a patient-specific maximum-tolerated activity treatment planning algorithm for 188Re-lipiodol therapy of liver cancer can be implemented and largely automated.

References